1 Past Papers

- 2001 Paper 4 Question 4
- 2007 Paper 4 Question 4

2 Practical

You are given a basic compiler for a very simple language, which supports integers and closures. Start by forking the following repository: https://github.com/nandor/mini-lambda. If you want me to comment on your code, please point me to your fork on GitHub!

2.1 Getting Started

Before implementing any features, ensure the compiler builds and runs correctly. If you encounter any issues, please contact me as soon as possible - or file an issue on GitHub.

- Install dependencies, starting with opam2: https://opam.ocaml.org/doc/Install.html
- Install dune, the build system: opam install dune
- Install menhir, the parser generator: opam install menhir
- Build the project: dune build main.exe
- Compile a file: ./lambda tests/full.lambda
- Read the comments inside the source files in the project

The lambda script is written in Bash - it invokes the compiler to generate an assembly source from an input written in the lambda language. The assembly file is compiled with the system assembler (usually gas on Linux, clang on macOS) and linked with the runtime, which provides some builtin methods performing I/O.

3 The Language

Presently, lambda supports functions, closures, integers and the addition operator. Functions which have no body, such as print_int in the example, are external methods implemented in assembly language by the runtime. Some examples can be found in the tests directory inside the project. Currently, there is no explicit syntax for type annotations: all types are inferred using the Hindley-Milner algorithm. The language is type-safe, with the exception of external methods (which you will fix!).

Exercise: Study the type checker in typing.ml and explain the similarities between the grouping of strongly connected components and let rec ... and in OCaml. Name an advantage and a disadvantage.

The compiler currently supports two targets: ARMv7 and x86_64. The compiled code is not particularly efficient - the instructions emulate a stack machine. On x86_64, the target which you will probably be using, the stack machine is implemented using the following registers:
• `%rax` stores the environment pointer of closures

• `%rbp` is the base pointer on the stack. The value located at the location pointed to by `%rbp` is the base pointer of the previous frame - this chain can be used to traverse all the stack frames. The value on the stack on top of the base pointer is the return address. Arguments follow: the i\textsuperscript{th} argument is located at `%rbp + 16 + 8 \times i`. Local variables are stored on the stack below `%rbp`: they can be accessed at `%rbp - (i + 8) \times 8`.

\textit{Exercise} Your first task is to draw a diagram of the stack layout, after studying the code generator.

• `%rsp` is the stack pointer: points to the bottom of the stack.

• `%rcx` and `%rdx` store temporary values for various computations. `%rcx` also stores the return value from a function call.

4 The Compiler

Compilation proceeds through the following stages, implemented in the files mentioned below:

• `lexer.mll`: Lexical analysis

• `parsing.mly`: The parser constructs the AST defined in `ast.ml`

• `typing.ml`: Implements type checking and produces a typed AST, defined in `typed_ast.ml`

• `ir_lowering.ml`: Generates the stack-based IR defined in `ir.ml`

• `backend*.ml`: Lowers the IR to machine code

5 The Task

Your task is to build up the features required to add conditional and looping constructs.

5.1 Subtraction

Due to the finite number of hours available in a day, the language seems to be lacking a subtraction operator. The first exercise involves implementing it, following the steps below:

1. Define a token in the parser, name it \texttt{MINUS}

2. Provide a rule in the lexer to consume the minus sign and generate the correct token

3. Define an AST node for subtraction

4. Add a rule to the parser to construct that AST node, similarly to the addition operator. If at any point the OCaml compiler complains about unimplemented patterns in match statements, stub them out with \texttt{failwith}

5. Add a type checking rule - should be a straightforward adaptation of the addition rule

6. Add an instruction to the IR in `ir.ml` to execute subtraction

7. Lower subtraction to the IR

8. Generate code - the instruction on \texttt{x86_64} is `subq`. Stub out the ARM version or implement it in case you have access to a board you can test on.

The previous steps highlight all the changes required to the compiler - make sure you get the hang of it as the following exercises will be less detailed.
5.2 Booleans

It is a good idea to be able to use boolean values as conditions to if statements and while loops. Add the following constants and operators to the language:

- `true`
- `false`
- `==`
- `!=`
- `&&`
- `||`

This time you will also need to add a new type, alongside `TyInt`. Unification should stay unchanged.

5.3 Assignment

What does the following bit of code achieve? How many copies of `x` will there be?

```plaintext
x <- 1;
x <- 2;
```

This is not particularly useful in an imperative language. Modify the compiler such that the second 'bind' to `x` rewrites the initial value instead of creating a new local.

5.4 If Statements

The language should support if statements with optional else branches. Implement them. In the IR and assembly, you will need at least the following 3 constructs:

- Labels: to denote a point in the program, used as target for jumps.
- Unconditional jumps: `jmp` in assembly.
- Conditional jumps: All jumps should take a boolean argument. Assuming one is on top of the stack prior to the jump, it can be popped into a register. Afterwards, `tstq %rdx, %rdx` can be used (with almost any register!) to check if the value is zero, followed by `jz` or `jnz`.

6 Additional Questions

1. Consider the following example from some awful programming language which shall remain unnamed:

```plaintext
function test(a, b, c) {
    return a + b / c.length - 123.0;
}
function some_call(c, d) {
    z = c + c;
    return test(3, z, "\"hello\" + d);
}
some_call(5, "world\\"");
```

(a) Enumerate all the tokens, grouping them by their type.

(b) Draw the automata which accept the following tokens: numbers, identifiers and strings.
(c) Provide regular expressions which match numbers, identifiers and strings.
(d) Constructs the NFAs of the previous regular expressions and reduce them to DFAs.
(e) Draw the automaton of the entire lexer, with states to accept all tokens of the language.
(f) Implement the lexer in ocamllex.

2. In some languages, floating point numbers can be defined in multiple ways. The following are examples of valid numeric constants in C++11:

- 0b101
- 0x123
- 0233
- 1234
- -123.5
- 123.5f
- 1.3e-20
- 2.3e+10
- 1e1f

(a) Provide a regular expression for the following: binary, decimal, hexadecimal, float and double.
(b) Draw an automaton with accepting states for the following tokens, capable of parsing numbers similar to the ones shown before, with 3 accepting states: INT, FLOAT, DOUBLE.
(c) Can you design a regex to only accept 32-bit signed integers? Sketch a solution. How about 32-bit floats? Explain why this might not be practical. How would you handle this in ocamllex?
(d) At what stage in the compiler should an error be emitted when a numeric constant is too large? Discuss the following languages: C/C++, Java, OCaml and JavaScript.

3. This question concerns parsing and representations.

(a) Define the Abstract Syntax Tree (AST) of the awful language mentioned before in OCaml, using records and variants. What are the options of representing function bodies and statements? Make sure the AST can represent first-class functions and closures.
(b) Draw the parse tree and the AST of the test function:

```ocaml
function test(a, b, c) {
    return a + b / c.length - 123.0;
}
```

(c) Provide the EBNF grammar for a parser.
(d) Sketch the code of a recursive descent parser for this grammar.

4. The awful language mentioned before also supports regular expressions with the following syntax:

```ocaml
function is_aaa(str) {
    return /aaa/.match(str);
}
```

(a) Write a function which contains the string /aaa/, but does not contain any regexes.
(b) Can you tokenize the stream by simply adding a rule to the previous lexer? Explain why not.
(c) Show how the recursive descent parser would interact with a modified lexer to parse this language.
5. Provide the small-step semantics of the language, with eager evaluation, passing arguments from left-to-right. Discuss any other assumptions. Show how the following example reduces to a single value:

```javascript
function f(x) {
    return function(z) {
        return x + z;
    };
};
f(2)(3)
```